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## Spin Accumulation and Spin Relaxation in a Large Open Quantum Dot

E. J. Koop,<sup>1</sup> B. J. van Wees,<sup>1</sup> D. Reuter,<sup>2</sup> A. D. Wieck,<sup>2</sup> and C. H. van der Wal<sup>1</sup>

<sup>1</sup>*Physics of Nanodevices Group, Zernike Institute for Advanced Materials, University of Groningen, Nijenborgh 4, NL-9747AG Groningen, The Netherlands*

<sup>2</sup>*Angewandte Festkörperphysik, Ruhr-Universität Bochum, D-44780 Bochum, Germany*

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We report electronic control and measurement of an imbalance between spin-up and spin-down electrons in micron-scale open quantum dots. Spin injection and detection were achieved with quantum point contacts tuned to have spin-selective transport, with four contacts per dot for realizing a nonlocal spin-valve circuit. This provides an interesting system for studies of spintronic effects since the contacts to reservoirs can be controlled and characterized with high accuracy. We show how this can be used to extract in a single measurement the relaxation time for electron spins inside a ballistic dot ( $\tau_{sf} \approx 300$  ps) and the degree of spin polarization of the contacts ( $P \approx 0.8$ ).

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The ability to control and detect the average spin orientation of electron ensembles in nonmagnetic conductors lies at the heart of spintronic functionalities [1]. We report here electronic control and detection of spin accumulation—an imbalance between the chemical potential of spin-up and spin-down electrons—in a large ballistic quantum dot in a GaAs heterostructure. We use quantum point contacts (QPCs) to operate a four-terminal quantum dot system, which is suited for realizing a nonlocal spin-valve circuit [2]. Before, such spin-valve circuits were realized with ferromagnetic contacts on various nonmagnetic conductors [2–4], but for these systems it is hard to characterize the contact properties. An interesting aspect of our spintronic system is that it is realized with ultraclean nonmagnetic materials, while each spin-selective mode in the contacts can be controlled individually. We demonstrate that this can be exploited to measure and unravel for a single device the spin-relaxation rate inside the dot, contributions to spin relaxation from coupling the dot to reservoirs, and the degree of polarization for spin-selective transport in the contacts. Thus, we report here the spin-relaxation time for two different confinement geometries. Chaotic scattering inside such ballistic cavities can result in a spin-relaxation mechanism that differs from that of bulk materials and very small few-electron quantum dots [5], but its full understanding is still a challenge to the community [6].

Figure 1(a) presents our device. Depletion gates on a heterostructure with a two-dimensional electron gas (2DEG) below the surface are used to define the four-terminal dot. QPCs are operated as spin-selective contacts, using the fact that the subbands that carry the ballistic transport can be Zeeman split with a strong in-plane magnetic field and that these modes can be opened up one by one by tuning gate voltages [7,8]. The conductance of QPCs then increases in steps, with plateaus at  $Ne^2/h$ , where  $N$  is the number of open modes. For odd (even)  $N$ , the last opened mode carries only spin-up (spin-down). For

the most typical form of our experiment, we tune to the following setting. The QPC to the  $I+$  reservoir has a single open mode, which is available only for spin-up electrons, while the  $I-$  QPC is tuned to carry one mode for spin-up and one for spin-down, and we apply here a current  $I_{\text{bias}}$ . The contact resistance for electrons entering the dot via  $I-$  is equal for spin-up and spin-down, while the current that leaves the dot carries only spin-up. Consequently, the chemical potential for spin-down electrons inside the dot will become higher than that for spin-up, up to a level that is limited by spin relaxation. This difference in chemical potential  $\Delta\mu_{\uparrow\downarrow}$  can be measured as a voltage: With the  $V+$  QPC tuned to have only one open mode for spin-up and the  $V-$  QPC tuned to have one open mode for spin-up and one for spin-down, the voltage is  $V = \Delta\mu_{\uparrow\downarrow}/2e$ , which is for

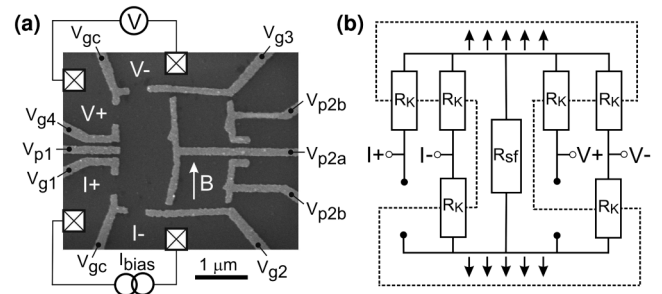


FIG. 1. (a) Electron microscope image of the device, with labels for current and voltage contacts, and depletion gates  $V_{gi}$  and  $V_{pi}$ . Gate  $V_{p1}$  is a shape-distorting gate. Fully switching gate  $V_{p2a}$  or gates  $V_{p2b}$  on or off sets the overall size of the dot, but fine-tuning these gates is also used for controlling small shape distortions. (b) Resistor model for the most typical experiment (see text), for the case of ideal spin polarization of the contacts to the  $I+$  and  $V+$  reservoirs. The spin-up (top) and spin-down (bottom) populations inside the dot are contained within the dashed line. The spin-flip resistance  $R_{sf}$  represents spin relaxation inside the dot.

linear response expressed as a nonlocal resistance  $R_{nl} = V/I_{bias}$ .

The resistor model in Fig. 1(b) is useful for analyzing how spin-relaxation mechanisms influence the measured signal in the above experiment. Each open mode for spin-up in a QPC is modeled as a resistor with value  $R_K = h/e^2$  to the spin-up population in the dot, and similar for spin-down (we assume first perfect polarization of QPCs tuned to be spin-selective). Spin relaxation *inside* the dot is modeled as a resistor  $R_{sf}$  that carries a current from the spin-up to the spin-down population. Figure 1(b) illustrates that the contacts to the  $I-$  and the  $V-$  reservoir provide additional current paths for relaxation parallel to  $R_{sf}$  (spins rapidly mix in reservoirs, and reservoirs always have zero spin accumulation). This mechanism for spin relaxation *outside* the dot causes, in the limit of  $R_{sf} \rightarrow \infty$  (no relaxation inside the dot),  $R_{nl}$  to be limited to  $R_K/4$ . The voltage that is driving the relaxation inside the dot is  $\Delta\mu_{\uparrow\downarrow}/e$ , while the current through  $R_{sf}$  is  $I_{sf} = e\Delta\mu_{\uparrow\downarrow}/2\Delta_m\tau_{sf}$ , such that the spin-flip time  $\tau_{sf}$  dictates  $R_{sf}$  according to  $R_{sf} = 2\tau_{sf}\Delta_m/e^2$  [9]. Here  $\Delta_m = 2\pi\hbar^2/m^*A$  is the mean energy spacing between spin-degenerate levels in a dot of area  $A$ . Consequently, measuring  $R_{nl}$  and deriving  $R_{sf}$  from its value can be used for determining  $\tau_{sf}$ . While this resistor model does not account for various mesoscopic effects that occur in ballistic chaotic quantum dot systems, a theoretical study of an equivalent two-terminal spintronic dot [6] showed that it is valid in the regime that applies to our experiment (no influence of weak-localization and Coulomb blockade effects), and we indeed find that it is consistent with the measured spin signals that we report.

The dot was realized in a GaAs/Al<sub>0.32</sub>Ga<sub>0.68</sub>As heterostructure with the 2DEG at 114 nm depth. At 4.2 K, the mobility was  $\mu = 159 \text{ m}^2/\text{Vs}$ , and the electron density  $n_s = (1.5 \pm 0.1) \times 10^{15} \text{ m}^{-2}$ . For gates we used electron-beam lithography and liftoff techniques and deposition of 15 nm of Au on a Ti sticking layer. The reservoirs were connected to wiring via Ohmic contacts, which were realized by annealing Au/Ge/Ni from the surface. All measurements were performed in a dilution refrigerator at an effective electron temperature  $T_{eff} \approx 100 \text{ mK}$ . For measuring  $R_{nl}$  we used lock-in techniques at 11 Hz with a current bias, where we made sure that the associated bias voltage  $V_{bias} \leq 10 \mu\text{V}$ . We carefully checked that RC effects did not influence  $R_{nl}$  results. We used the T-shaped gate  $V_{p2a}$  or pair of gates  $V_{p2b}$  for setting the *overall size* of the dot (not to be confused with tuning small shape distortions for averaging out fluctuations; see below) at an area of either 1.2 or 2.9  $\mu\text{m}^2$  (accounting for a depletion width of  $\sim 150 \text{ nm}$  around the gates).

Before presenting measurements of spin accumulation, we discuss two effects that make this experiment in practice less straightforward than in the above description. Quantum fluctuations in  $R_{nl}$  due to electron interference inside the dot [10] have an amplitude that is comparable to

the spin signal [11], and  $R_{nl}$  can be studied as a spin signal only after averaging over a large number of fluctuations. The inset in Fig. 2(a) shows such fluctuations in  $R_{nl}$  as a function of the voltage on  $V_{p1}$ , which causes a small shape distortion of the dot. We discuss results as  $\langle R_{nl} \rangle$  when presenting the average of 200 independent  $R_{nl}$  fluctuations, from sweeping with two different shape-distorting gates. Cross talk effects between gates were carefully mapped out and compensated for keeping the QPCs at their desired set points [12].

A second effect which, besides spin accumulation, may result in strong  $R_{nl}$  values is electron focusing [11]. Our sample was mounted with its plane at  $0.73^\circ$  with respect to the direction of the total magnetic field  $B$ . Consequently, there is a small perpendicular field  $B_{\perp}$ , and the associated electron cyclotron diameter equals the  $I+$  to  $V+$  contact distance [Fig. 1(a)] at  $B = \pm 6 \text{ T}$ . We will mainly present results measured at  $B = +8.5 \text{ T}$ , for which we found that focusing only weakly influences  $\langle R_{nl} \rangle$  results. Further, we use the fact that we can subtract a background contribution to  $\langle R_{nl} \rangle$  from focusing (discussed below), and we present results where this is applied as  $\langle R_{nl} \rangle_{fc}$ .  $B_{\perp}$  also breaks time-reversal symmetry (suppressing weak localization) when  $|B| > 0.2 \text{ T}$ .

Figure 2(a) presents  $\langle R_{nl} \rangle_{fc}$  as a function of the number of open modes in the  $I+$  contact (tuned by  $V_{g1}$ ), while the

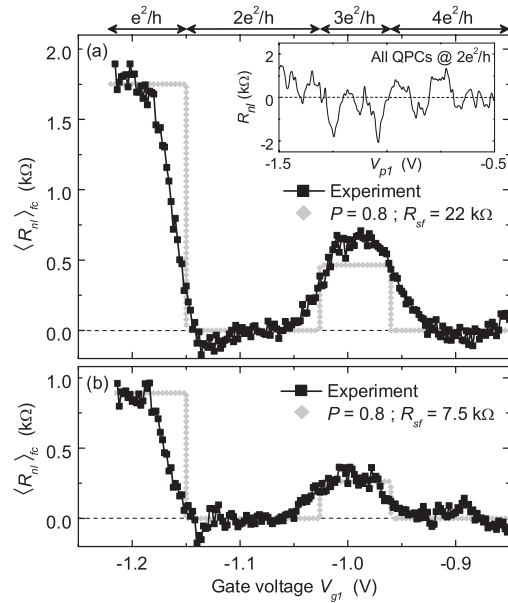


FIG. 2. (a) Nonlocal resistance results  $\langle R_{nl} \rangle_{fc}$  as a function of gate voltage  $V_{g1}$  (controlling the number of open modes in the  $I+$  QPC, corresponding conductance plateaus are indicated at the top axis) for the dot with area (a) 1.2 and (b) 2.9  $\mu\text{m}^2$ , measured at  $B = +8.5 \text{ T}$ . Gray lines show  $R_{nl}$  values from the resistor model, with the spin-flip resistance  $R_{sf}$  and polarization  $P$  as in the figure labels. The inset in (a) shows fluctuations of  $R_{nl}$  as a function of shape gate  $V_{p1}$  with all QPCs at a conductance of  $2e^2/h$ .

other QPCs are tuned as in Fig. 1(b). On the left on this  $V_{g1}$  axis, the  $I+$  QPC carries only one spin-up mode (conductance  $G_{I+}$  tuned to the  $e^2/h$  plateau; see also top axis). Here  $\langle R_{nl} \rangle_{fc} \approx 1.8 \text{ k}\Omega$ . Tuning  $V_{g1}$  to more positive values first adds an open spin-down mode to the  $I+$  QPC ( $G_{I+}$  at  $2e^2/h$ ), such that it is no longer spin-selective and  $\langle R_{nl} \rangle_{fc}$  drops here indeed to values near zero. Further opening of the  $I+$  QPC tunes it to have two spin-up modes in parallel with one spin-down mode ( $G_{I+} = 3e^2/h$ ). This causes again a situation with more spin-up than spin-down current in the  $I+$  QPC, but less distinct than before, and here  $\langle R_{nl} \rangle_{fc}$  shows again a clear positive signal. Then it drops to zero once more when the next spin-down mode is opened in the QPC. We obtain nominally the same results when the role of the current and voltage contacts is exchanged. Further, Fig. 2(b) shows that the large dot shows the same behavior but with lower  $\langle R_{nl} \rangle_{fc}$  values. This agrees with a lower value for  $R_{sf}$  for the large dot. From these measurements we can conclude that  $\langle R_{nl} \rangle_{fc}$  is a signal that is proportional to the spin accumulation  $\Delta\mu_{\uparrow\downarrow}$  in the dot.

Figure 3 shows results from a similar experiment on the small dot (but also here the large dot showed the same behavior). Now  $\langle R_{nl} \rangle_{fc}$  is measured as a function of the number of open modes in the  $V-$  QPC (tuned by  $V_{g3}$ ), while all other QPCs are again tuned as in Fig. 1(b). Here we observe a signal close to zero when the  $V-$  QPC carries only one spin-up mode ( $G_{V-} = e^2/h$ ) since it then probes the same chemical potential as the  $V+$  QPC. Opening it to  $G_{V-} = 2e^2/h$  immediately results in a strong signal. Further opening this QPC then causes the signal to go up and down, qualitatively in reasonable agreement with the resistor model that assumes perfect polarization ( $P = 1$ ) of each spin-selective mode in a QPC (see theory traces in Fig. 3; these go up and down in a steplike manner since we assume sharp transitions between conductance plateaus). However, with quantitative agreement at  $G_{V-} = 2e^2/h$

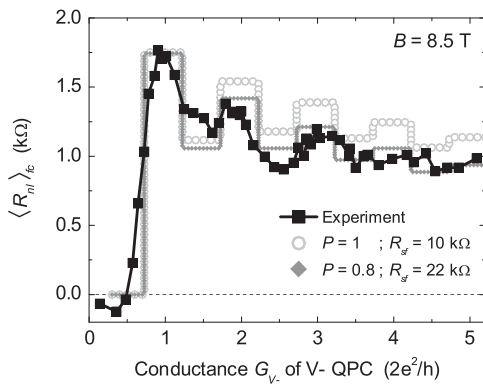


FIG. 3. Averaged nonlocal resistance  $\langle R_{nl} \rangle_{fc}$  as a function of the conductance  $G_{V-}$  of the  $V-$  QPC, for  $A = 1.2 \mu\text{m}^2$ . Gray lines show  $R_{nl}$  values from the resistor model, with the spin-flip resistance  $R_{sf}$  and polarization  $P$  as labeled.

(for  $R_{sf} = 10 \text{ k}\Omega$ ), this model with  $P = 1$  shows an average slope down with increasing  $G_{V-}$  that is too weak. Instead, we find that the resistor model can show quantitative agreement over the full  $G_{V-}$  range (and with the results in Fig. 2) when we account for imperfect spin polarization of QPCs.

We model imperfect polarization in the resistor model as follows. We assume it plays a role only for QPCs set to a conductance of  $Ne^2/h$ , with  $N$  an odd integer (because the energy spacing between pairs of Zeeman-split subbands is large [8]). Spin-selective transport is then only due to the highest pair of subbands that contributes to transport, and we define the polarization  $P$  only with respect to this pair. This pair of subbands is then modeled as a resistor  $R_{\uparrow} = 2R_K/(1 + P)$  to the spin-up population in the dot and a resistor  $R_{\downarrow} = 2R_K/(1 - P)$  to the spin-down population, which corresponds to  $P = (R_{\downarrow} - R_{\uparrow})/(R_{\downarrow} + R_{\uparrow})$ . This provides a simple model for  $R_{nl}$  with only  $R_{sf}$  and  $P$  as fitting parameters if we assume that all spin-selective QPCs and QPC settings can be modeled with a single  $P$  value. We find then a good fit to all of the data in Figs. 2 and 3 for  $P = 0.8 \pm 0.1$ , with  $R_{sf} = 22 \pm 3 \text{ k}\Omega$  for the small dot and  $R_{sf} = 7.5 \pm 1 \text{ k}\Omega$  for the large dot. In Fig. 2(a) at  $G_{I+} = 3e^2/h$ , the experimental results are higher than the plotted model values. However, this turns into the opposite situation when using results obtained with the current and voltage QPCs exchanged. This indicates that  $P$  does not have exactly the same value for all QPCs and QPC settings. There is, however, always agreement with the model when accounting for the error bars of  $P$  and  $R_{sf}$ .

The values of  $R_{sf}$  correspond to  $\tau_{sf} = 295 \pm 40 \text{ ps}$  for the small dot and  $\tau_{sf} = 245 \pm 35 \text{ ps}$  for the large dot. In our type of system, spin relaxation in the dot is probably dominated by Rashba and Dresselhaus spin-orbit coupling. How this mechanism results in a certain value for  $\tau_{sf}$  then depends on the ballistic scattering rate at the edge of the dot. We performed numerical simulations of this mechanism, which yield the fact that relaxation times indeed depend on the size of the dot, with typical values near  $300 \text{ ps}$  [5]. In our experiment, however, the error bars for  $\tau_{sf}$  are too large for studying this dependence on the shape of our dots, but our method is suited for exploring this topic in future work.

Figure 4 shows how focusing affects  $\langle R_{nl} \rangle$  and  $\langle R_{nl} \rangle_{fc}$ . For QPCs tuned as in Fig. 1(b), the signal from spin accumulation drops to zero if either the  $I+$  or the  $V+$  QPC is tuned from  $e^2/h$  to  $2e^2/h$  (no longer spin-selective). However, when sweeping  $B$  we also measure large positive and negative  $\langle R_{nl} \rangle$  values when the  $I+$  QPC, the  $V+$  QPC, or both are at  $2e^2/h$ . For these three settings, we observed  $\langle R_{nl} \rangle$  traces that are nominally the same [black symbols in Fig. 4(a)]. The peaked structure is due to electron focusing effects [7,11]. Only the peak at  $+6 \text{ T}$  corresponds to direct focusing from the  $I+$  into the  $V+$  contact without an intermediate scatter event on the edge of



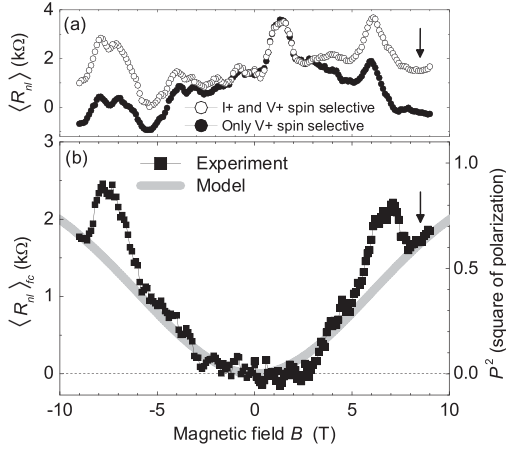


FIG. 4. (a) Averaged nonlocal resistance  $\langle R_{nl} \rangle$  as a function of  $B$ , for  $I+$  and  $V+$  at the  $e^2/h$  spin-polarized conductance plateau (open symbols) and for  $I+$  at  $2e^2/h$  (not spin-selective) and only  $V+$  at  $e^2/h$  (solid symbols). The  $I-$  and  $V-$  QPCs are at  $2e^2/h$ ,  $A = 1.2 \mu\text{m}^2$ . The difference in  $\langle R_{nl} \rangle$  for the traces in (a) defines the focusing corrected nonlocal resistance  $\langle R_{nl} \rangle_{fc}$ , shown in (b). The gray line in (b) is a fit of the model where the polarization  $P$  of QPCs (right axis) increases with Zeeman splitting (see text). Arrows indicate  $B$  that was applied for measuring the data of Figs. 2 and 3.

the dot (it has the right  $B$  value, and other peaks move to other  $B$  values when comparing the small and the large dots). Note, however, that all  $\langle R_{nl} \rangle$  values are significantly higher when both the  $I+$  and the  $V+$  QPC are tuned to be spin-selective [open symbols in Fig. 4(a)]. This difference between the open and black symbols defines the quantity  $\langle R_{nl} \rangle_{fc}$  [Fig. 4(b)] and provides a signal that is mainly due to spin. These  $\langle R_{nl} \rangle_{fc}$  data also show a peaked structure where  $\langle R_{nl} \rangle$  shows strong focusing signals. This agrees with enhancement of electron focusing signals between spin-selective QPCs [7].

For interpreting  $\langle R_{nl} \rangle_{fc}$  as a measure for spin accumulation, the experiment must be performed in a regime with many chaotic scatter events inside the dot during the electron dwell time. This is clearly not the case at the focusing peaks in Fig. 4(b) (at  $-7.5$  and  $+6$  T). We therefore studied spin accumulation at  $+8.5$  T, where focusing from the  $I+$  QPC scatters on the edge of the dot just before the  $V+$  contact and where the signatures of focusing in  $\langle R_{nl} \rangle$  are small. The agreement between the results of both Figs. 2 and 3, for both the small and the large dot, and the resistor model supports the conclusion that these results were obtained in a chaotic regime.

As a final point, we discuss the fact that the degree of polarization  $P = 0.8$  is in agreement with independently determined QPC properties. Steps between conductance plateaus are broadened by thermal smearing (a very weak contribution for our QPCs at 100 mK) and due to tunneling and reflection when the Fermi level  $E_F$  is close to the top of the QPC potential barrier for the mode that is opening. It is

mainly this latter effect that causes  $P < 1$  in our experiments. The role of tunneling and reflection in QPC transport is described with an energy-dependent transmission  $T(\epsilon)$  that steps from 0 to 1 when a QPC mode is opened. We study the effect of this on  $P$  by assuming that  $E_F$  is located exactly between the bottoms of a pair of Zeeman-split subbands. For these two subbands we use  $T(\epsilon)_{\uparrow(\downarrow)} = (\text{erf}\{\alpha[\epsilon - E_F - (+)E_Z/2]\} + 1)/2$ , a phenomenological description that agrees with studies of our QPCs [8]. Here  $E_Z = g\mu_B B$  is the Zeeman splitting (for  $g$  factor  $g$  and Bohr magneton  $\mu_B$ ) and  $\alpha$  a parameter that sets the width of the step in  $T(\epsilon)$ . For  $eV_{\text{bias}} < k_B T_{\text{eff}}$ , the contributions of these two subbands to the QPC conductance are then  $G_{\uparrow(\downarrow)} = (e^2/h) \int d\epsilon (-df/d\epsilon) T(\epsilon)_{\uparrow(\downarrow)}$ , where  $f$  is the Fermi function. With  $P = (G_{\uparrow} - G_{\downarrow})/(G_{\uparrow} + G_{\downarrow})$  we now calculate how  $P$  increases with  $B$  due to an increasing Zeeman splitting. In the resistor model, the dependence of  $R_{nl}$  on  $P$  is close to  $R_{nl} \propto P^2$ . We therefore plot  $P^2$  in Fig. 4(b) (gray line, with scaling of the right axis such that it overlaps with the experimental results) for parameters that give the consistent result  $P = 0.8$  at  $B = 8.5$  T. For this, we use  $|g| = 0.44$  (as for bulk GaAs) and an  $\alpha$  value that is derived from a FWHM of 0.2 meV for the peak in  $dT(\epsilon)/d\epsilon$ . The latter parameter agrees with the values 0.20–0.35 meV that we found when characterizing this for our QPCs [8]. Notably, we cannot calculate such a consistent result if we assume that the many-body effects that we observed in our QPCs [8] enhance the Zeeman splitting (showing, for example,  $|g| \approx 1.1$ ). This indicates that these effects do not play a role for spin injection and detection with QPCs, as was also found in Ref. [7].

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*Note added.*—We have been made aware of related results by Frolov *et al.* [13] with a narrow Hall bar and Zumbühl *et al.* with a two-terminal dot [14].

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